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## Sigma Convergence versus Beta Convergence: Evidence from U.S. County-Level Data

In this paper, we outline (i) why  $\sigma$ -convergence may not accompany  $\beta$ -convergence, (ii) discuss evidence of  $\beta$ -convergence in the United States, and (iii) use U.S. county-level data containing over 3,000 cross-sectional observations to demonstrate that  $\sigma$ -convergence cannot be detected at the county level across the United States, or within the large majority of the individual U.S. states considered separately. Indeed, in many cases statistically significant  $\sigma$ -divergence is found.

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ONE CAN DISTINGUISH between two types of convergence in growth empirics:  $\sigma$ -convergence and  $\beta$ -convergence. When the dispersion of real per capita income (henceforth, simply “income”) across a group of economies falls over time, there is  $\sigma$ -convergence. When the partial correlation between growth in income over time and its initial level is negative, there is  $\beta$ -convergence.

By the “convergence literature,” economists typically refer to the large literature, typified by the seminal papers by Barro and Sala-i-Martin (1992) and Mankiw et al. (1992), exploring  $\beta$ -convergence. Sala-i-Martin (1996, p. 1326), surveying this

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literature, concludes that “the estimated speeds of [ $\beta$ -]convergence are so surprisingly similar across [cross-sectional] data sets, that we can use a mnemonic rule: *economies converge at a speed of two percent per year.*” In other words, economies close the gap between present levels of income and balanced growth levels by, on average, 2% annually. Panel data studies find even higher rates of  $\beta$ -convergence (see Islam 1995, Evans 1997a) as do the county-level U.S. studies of Higgins et al. (2006) and Young et al. (2007).

Despite the literature’s stress on  $\beta$ -convergence, economists have acknowledged that it is not a sufficient condition for  $\sigma$ -convergence (for an early acknowledgment of this idea see Barro and Sala-i-Martin 1992, pp. 227–28). Indeed, Quah (1993) and Friedman (1992) both suggest that  $\sigma$ -convergence is of greater interest because it speaks directly as to whether the distribution of income across economies is becoming more equitable.

In this paper, we demonstrate that  $\beta$ -convergence is a necessary but *not* sufficient condition for  $\sigma$ -convergence. Then, we discuss evidence of  $\beta$ -convergence in the United States using county-level data covering 1970–1998 and containing over 3,000 cross-sectional observations. We demonstrate, using the same data, that  $\sigma$ -convergence cannot be detected during that time period in the United States or within the large majority of the individual U.S. states considered separately. Indeed, in many cases statistically significant  $\sigma$ -divergence is found.

The paper is organized as follows. Section 1 demonstrates why  $\sigma$ -convergence need not accompany  $\beta$ -convergence. Section 2 describes the U.S. county-level data that are the basis for our present ( $\sigma$ -convergence) and previously reported ( $\beta$ -convergence) results. Section 3 discusses the existing empirical evidence indicating that  $\beta$ -convergence exists in the United States. Section 4 demonstrates that  $\sigma$ -convergence did not occur across the United States, or within a majority of the individual U.S. states, from 1970 to 1998. Section 5 reports Gini coefficients for the same county-level data that are consistent with a lack of  $\sigma$ -convergence. Section 6 concludes.

## 1. $\beta$ -CONVERGENCE VERSUS $\sigma$ -CONVERGENCE

Following Sala-i-Martin’s (1996) exposition, assume that  $\beta$ -convergence holds for economies  $i = 1, \dots, N$ .<sup>1</sup> Natural log-income of the  $i$ th economy can be approximated by

$$\ln(y_{it}) = a + (1 - \beta) \ln(y_{i,t-1}) + u_{it}, \quad (1)$$

1. Barro and Sala-i-Martin (1995) present a similar exposition and intuitive discussion. More recently, Furceri (2005) presents a related demonstration based on an OLS estimator of the coefficient on initial income.

where  $0 < \beta < 1$  and  $u_{it}$  has mean zero, finite variance,  $\sigma_u^2$ , and is independent over  $t$  and  $i$ . Because  $a$  is assumed constant across economies, balanced growth paths are identical.<sup>2</sup>

Manipulating equation (1) yields,

$$\ln\left(\frac{y_{it}}{y_{i,t-1}}\right) = a - \beta \ln(y_{i,t-1}) + u_{it}. \tag{1}'$$

Thus,  $\beta > 0$  implies a negative correlation between growth and initial log income.

The sample variance of log income in  $t$  is given by

$$\sigma_t^2 = \left(\frac{1}{N}\right) \sum_{i=1}^N [\ln(y_{it}) - \mu_t]^2, \tag{2}$$

where  $\mu_t$  is the sample mean of (log) income. The sample variance is close to the population variance when  $N$  is large, and equation (1) can be used to derive the evolution of  $\sigma_t^2$ :

$$\sigma_t^2 \cong (1 - \beta)^2 \sigma_{t-1}^2 + \sigma_u^2. \tag{3}$$

Only if  $0 < \beta < 1$  is the difference equation stable, so  $\beta$ -convergence is necessary for  $\sigma$ -convergence.<sup>3</sup> Given  $0 < \beta < 1$ , the steady-state variance is

$$(\sigma^2)^* = \frac{\sigma_u^2}{[1 - (1 - \beta)^2]}. \tag{4}$$

Thus, the cross-sectional dispersion falls with  $\beta$  but rises with  $\sigma_u^2$ . Combining equations (3) and (4) yields

$$\sigma_t^2 = (1 - \beta)^2 \sigma_{t-1}^2 + [1 - (1 - \beta)^2](\sigma^2)^*, \tag{5}$$

which is a first-order linear difference equation with constant coefficients. Its solution is given by

$$\sigma_t^2 = (\sigma^2)^* + (1 - \beta)^{2t} [\sigma_0^2 - (\sigma^2)^*] + c(1 - \beta)^{2t}, \tag{6}$$

where  $c$  is an arbitrary constant. Thus, as long as  $0 < \beta < 1$ , we have  $|1 - \beta| < 1$ , which implies that

2. This is the case of *absolute*  $\beta$ -convergence; average growth rates of poor economies are unambiguously greater than those of rich economies. Allowing for different  $a_i$ s,  $0 < \beta < 1$  would imply the case of *conditional*  $\beta$ -convergence; the average growth rate of an economy is an *increasing function of its distance from its balanced growth level of income*. This is a weaker case of  $\beta$ -convergence and increases the set of possible scenarios where it does not imply  $\sigma$ -convergence. See the discussion at the end of this section.

3. If  $\beta \leq 0$ , the variance increases over time. If  $\beta = 1$ , the variance is constant, and if  $\beta > 1$ , the partial correlation between (log) income and its previous-period value would be negative and the series would oscillate, potentially from positive to negative values and back (making little economic sense).

$$\lim_{t \rightarrow \infty} (1 - \beta)^{2t} = 0. \quad (7)$$

This ensures the stability of  $\sigma_t^2$  because it implies that

$$\lim_{t \rightarrow \infty} \sigma_t^2 = (\sigma^2)^*. \quad (8)$$

Moreover, as  $(1 - \beta) > 0$ , the approach to  $(\sigma^2)^*$  is monotonic.

It follows, therefore, that the variance will increase or decrease toward its steady-state value depending on the initial  $\sigma_0^2$ . Intuitively, economies can be  $\beta$ -converging toward one another while, at the same time, random shocks are pushing them apart. Despite  $\beta$ -convergence, if the initial dispersion of income levels is, by chance, small relative to the variance of random shocks then the dispersion of incomes will converge toward its steady-state value from below.<sup>4</sup>

Other scenarios where  $\beta$ -convergence does not imply  $\sigma$ -convergence arise when the parameter  $a$  varies across economies.<sup>5</sup> Intuitively, consider two economies, A and B, where both economies begin at the same level of income. However, assume that B begins on its balanced growth path while A begins far below its balanced growth path, and assume that  $\beta$ -convergence holds. The initial variance ( $\sigma_0^2$ ) will be zero, but  $\sigma_t^2$  will grow over time as A grows faster than B and approaches a higher balanced growth path. Indeed,  $\beta$ -convergence is the reason for the increasing variance.<sup>6</sup>

## 2. U.S. COUNTY-LEVEL DATA

This paper utilizes the U.S. county-level data used by Higgins et al. (2006) and Young et al. (2007) to study income growth from 1970 to 1998. The data set includes 3,058 county-level observations and 50 individual state samples of various sizes, also at the county level (see Figure 1).

The personal income measure we use is the definition used by the U.S. Bureau of Economic Analyses (BEA). It is adjusted to be net of government transfers and is expressed in per capita 1992 dollars using the U.S. GDP deflator. Population measures from the U.S. Census are used to construct per capita amounts. Real per capita income levels are expressed as natural logs and values are considered for both 1970 and 1998.<sup>7</sup>

4. Note in equation (6) that the parameter  $\beta$  governs the speed at which the variance approaches its steady-state value because, according to equation (1), it governs how long the effect of shocks persist.

5. This represents the case of conditional  $\beta$ -convergence. In empirical applications the  $a_i$ s are often modeled as linear functions of various economic and/or socio-demographic variables available to the researcher (e.g., see Table 1 in Higgins et al. 2006).

6. In real economies,  $\sigma$ -convergence would also depend on whether or not disturbances are correlated, and have constant variances, across time and economies.

7. For a more detailed discussion of the data, see Higgins et al. (2006) or a data appendix available from the authors upon request. Also, see U.S. BEA (2001) for the personal income data concept and data gathering methods. The original data set contained 3,066 observations. Eight counties, however, were excluded from the data set for lack of data.

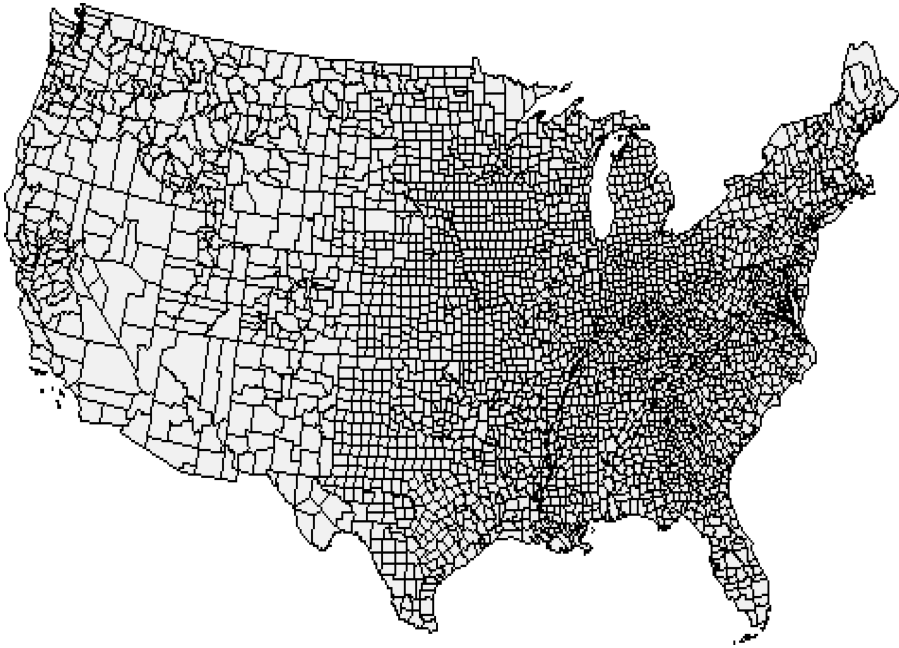


FIG. 1. 3,058 U.S. Counties.

NOTE: Not shown in the figure, but included in the analysis, are the counties of Alaska and Hawaii.

The definitions that are used for the components of personal income at the county level are essentially the same as those used for national measures.<sup>8</sup> For example, the BEA defines “personal income” as the sum of wage and salary disbursements, other labor income, proprietors’ income (with inventory valuation and capital consumption adjustments), rental income (with capital consumption adjustment), personal dividend income, and personal interest income.

### 3. $\beta$ -CONVERGENCE: EXISTING EVIDENCE

Many studies have documented  $\beta$ -convergence in the United States. Barro and Sala-i-Martin (1992), Evans and Karras (1996a, 1996b), Sala-i-Martin (1996), and Evans (1997a, 1997b) find statistically significant  $\beta$ -convergence effects using U.S. state-level data. The present authors use U.S. county-level data to document statistically significant  $\beta$ -convergence effects across the United States (Higgins et al. 2006) and within many individual U.S. states in and of themselves (Young et al. 2007) (see Table 1).

8. The data and their measurement methods are described in detail in “Local Area Personal Income, 1969–1992” published by the BEA under the Regional Accounts Data, February 2, 2001.

TABLE 1  
ASYMPTOTIC  $\beta$ -CONVERGENCE RATES—POINT ESTIMATES and 95% CONFIDENCE INTERVALS

State	Number of counties	OLS estimates and 95% CI	3SLS estimates and CI
United States	3,058	0.0239 (0.0224, 0.0255)	0.0658 (0.0632, 0.0981)
Alabama	67	0.0424 (0.0036, 0.1080)	0.0931 (0.0492, 0.1466)
Arkansas	74	0.0479 (0.0166, 0.1098)	0.0738 (0.0570, 0.1363)
California	58	0.0457 (0.0046, 0.1249)	0.0375 (0.0178, 0.0868)
Colorado	63	0.0166 (0.0031, 0.0384)	0.0759 (0.0426, 0.1009)
Florida	67	0.0268 (0.0010, 0.1109)	0.0767 (0.0480, 0.1174)
Georgia	159	0.0230 (0.0109, 0.0413)	0.1043 (0.0699, 0.1142)
Idaho	44	0.0892 (0.0021, 0.1566)	0.0913 (0.0471, 0.1145)
Illinois	102	0.0434 (0.0213, 0.1168)	0.0537 (0.0337, 0.1062)
Indiana	92	0.0067 (−0.0054, 0.0245)	0.0622 (0.0354, 0.1221)
Iowa	99	0.0570 (0.0224, 0.1176)	0.0574 (0.0175, 0.0954)
Kansas	106	0.0560 (0.0360, 0.1086)	0.0639 (0.0434, 0.1228)
Kentucky	120	0.0431 (0.0233, 0.0922)	0.1054 (0.0561, 0.1160)
Louisiana	64	0.0341 (0.0128, 0.0955)	0.1555 (0.0989, 0.1940)
Michigan	83	0.0121 (−0.0043, 0.0427)	0.1152 (0.0536, 0.1659)
Minnesota	87	0.0202 (0.0053, 0.0459)	0.0454 (0.0305, 0.0719)
Mississippi	82	0.0249 (0.0009, 0.1509)	0.1405 (0.0455, 0.1923)
Missouri	115	0.0230 (0.0094, 0.0452)	0.0817 (0.0387, 0.1132)
Montana	56	0.0359 (0.0099, 0.0996)	0.0865 (0.0367, 0.1566)
New York	62	0.0111 (−0.0238, 0.0284)	0.0465 (0.0285, 0.0853)
North Carolina	100	0.0228 (0.0078, 0.0491)	0.1302 (0.0966, 0.1574)
North Dakota	53	0.0528 (0.0103, 0.1247)	0.0761 (0.0353, 0.1102)
Ohio	88	0.0170 (−0.0005, 0.0520)	0.0503 (0.0299, 0.1059)
Oklahoma	77	0.0415 (0.0139, 0.1136)	0.1152 (0.0574, 0.1437)
Pennsylvania	67	0.0240 (0.0043, 0.0707)	0.0705 (0.0291, 0.1099)
South Carolina	46	0.0142 (−0.0147, 0.1259)	0.0960 (0.0243, 0.1315)
South Dakota	66	0.0274 (0.0250, 0.0300)	0.0406 (0.0184, 0.1144)
Tennessee	97	0.0287 (0.0102, 0.0689)	0.0681 (0.0488, 0.1168)
Texas	254	0.0312 (0.0208, 0.0458)	0.1170 (0.0675, 0.1564)
Virginia	84	0.0047 (−0.0074, 0.0227)	0.0703 (0.0500, 0.1271)
Washington	39	0.0518 (−0.0119, 0.0971)	0.0845 (0.0448, 0.1449)
West Virginia	55	0.0040 (−0.0184, 0.0199)	0.0634 (0.0466, 0.0972)
Wisconsin	70	0.0270 (0.0077, 0.0716)	0.0390 (0.0231, 0.0688)

NOTES: Estimates are results originally reported in Higgins et al. (2006) and Young et al. (2007). Following Evans (1997b, fn. 17, p. 16), we used  $c = 1 - (1 + T\beta)^{1/T}$  to compute the asymptotic rate of convergence. The confidence intervals (in parentheses) were obtained in two steps. First, we obtained the end points of the  $\beta$  confidence intervals by computing the interval  $\beta \pm (1.96\sigma_\beta)$ , where  $\sigma_\beta$  is the standard error associated with the estimate of  $\beta$ . Next, these endpoints were substituted into the expression,  $c = 1 - (1 + T\beta)^{1/T}$ . If the low value of the confidence interval was less than  $-T^{-1}$ , then the higher value was set equal to unity. It is clear from the above that the confidence intervals computed using this procedure may be asymmetric around the point estimates.

Using a consistent three-stage least squares (3SLS) estimation method, we estimate the  $\beta$ -convergence rate to be between 6.3% and 9.8% for the United States as a whole and, for individual U.S. states,  $\beta$ -convergence rate point estimates range from just under 4% (California) to over 14% (Louisiana) (see Table 1, column 3). Even considering ordinary least squares (OLS) estimates,  $\beta$ -convergence rate estimates are always positive when significant (see Table 1, column 2).

Clearly, considerable evidence supports the existence of  $\beta$ -convergence, which is a necessary condition for  $\sigma$ -convergence. Below we explore whether or not  $\sigma$ -convergence is occurring in the United States using the same county-level data that were used by Higgins et al. (2006) and Young et al. (2007).

#### 4. $\sigma$ -CONVERGENCE

To our knowledge, the only study of U.S. regional  $\sigma$ -convergence is Tsionas (2000). He examines real gross state products (RGSPs) and finds that “the cross sectional variance has fluctuated very little in the 20-year period from 1977 to 1996” (pp. 235–36). In contrast to Tsionas’ data set, our data cover nearly a decade longer. Moreover, we have over 3,000 county-level cross-sectional observations while Tsionas uses 50 state-level observations.<sup>9</sup> It turns out, nevertheless, that our findings are ultimately consistent with Tsionas’.

Table 2 reports 1970 and 1998 cross-sectional standard deviations of (log) income for the entire sample of U.S. counties and for each of the 50 U.S. states, and the associated  $p$ -values for a variance ratio test of the null that the ratio of the 2 standard deviations is unity (against the two-tailed alternative). The 1998 standard deviation for the full United States, sample (0.2887) is about 5.8% greater than that of 1970 (0.2728), a difference that is significant at the 1% level. In only 2 out of 50 states (Kansas and Oklahoma) is the 1998 standard deviation significantly less than that of 1970 (at the 10% level or better).<sup>10</sup> On the other hand, for 24 states the 1998 standard deviation is significantly larger (at the 10% level or better). Thus, for many individual states, as well as for the full United States,  $\sigma$ -divergence occurred from 1970 to 1998.<sup>11</sup>

Some have suggested that interpreting measures of dispersion may not be straightforward if the distributions are not unimodal (e.g., Quah 1997, Desdoigts 1999). However, as Figure 2 demonstrates, for the U.S. county-level data the distribution of income is unimodal for both 1970 and 1998. Figure 2 also allows one to confirm, visually, that  $\sigma$ -convergence is not present.

#### 5. HAS $\sigma$ -DIVERGENCE IMPLIED GREATER INCOME INEQUALITY?

Another measure we report that is associated with  $\sigma$ -convergence (in the sense that it deals with the distribution of income) is the Gini coefficient associated with U.S. counties’ 1970 and 1998 (log) incomes: 0.0167 and 0.0165, respectively—a decrease of about 1.2% (see Table 3). Recall that the Gini coefficient is a number between 0 (perfect equality) and 1 (perfect inequality).

Interestingly, at the county level, although the distribution of U.S. per capita income became a bit more dispersed from 1970 to 1998, it became a bit more equal.<sup>12</sup> However, the change in both the standard deviation and the Gini coefficient are small enough to suggest that both dispersion and equality remained essentially the same.

9. As well, Tsionas (2000) apparently did not convert RGSPs into per capita measures.

10. There is one other state where the standard deviation is smaller for 1998: Kentucky.

11. Of note, of the 24 states with statistically significant increases in standard deviations, 16 of them appear in Table 1 for having statistically significant  $\beta$ -convergence effects.

12. This statement is not to be confused with one concerning the distributions of U.S. *individuals’* incomes.

TABLE 2  
STANDARD DEVIATIONS OF U.S. COUNTIES' LOG PER CAPITA INCOMES, 1970 vs. 1998

Region	Number of counties	1970 per capita income standard deviation	1998 per capita income standard deviation	<i>p</i> -value
United States	3,058	0.2728	0.2887	0.0017
Alabama	67	0.1949	0.2073	0.6184
Alaska	9	0.4785	0.4798	0.9940
Arizona	9	0.2136	0.2987	0.2400
Arkansas	74	0.1904	0.1911	0.9900
California	58	0.1646	0.3328	0.0000
Colorado	63	0.2862	0.3282	0.2836
Connecticut	8	0.1491	0.2411	0.2283
Delaware	3	0.2062	0.2886	0.6759
Florida	67	0.2575	0.3360	0.0322
Georgia	159	0.2065	0.2304	0.0850
Hawaii	4	0.1513	0.2441	0.5555
Idaho	44	0.2003	0.2098	0.7619
Illinois	102	0.2044	0.2263	0.3086
Indiana	92	0.1263	0.1819	0.0006
Iowa	99	0.1089	0.1415	0.0049
Kansas	106	0.2279	0.1804	0.0303
Kentucky	120	0.3171	0.3151	0.9559
Louisiana	64	0.2195	0.2389	0.5034
Maine	16	0.1233	0.2002	0.0699
Maryland	24	0.2213	0.2927	0.1879
Massachusetts	14	0.1355	0.2155	0.0533
Michigan	83	0.1966	0.2663	0.0066
Minnesota	87	0.1887	0.1963	0.7168
Mississippi	82	0.1929	0.2464	0.0289
Missouri	115	0.2408	0.2464	0.8072
Montana	56	0.1870	0.1911	0.8716
Nebraska	93	0.1645	0.3475	0.0000
Nevada	17	0.1853	0.2150	0.5594
New Hampshire	10	0.0941	0.1444	0.2180
New Jersey	20	0.1379	0.2768	0.0030
New Mexico	32	0.2770	0.3055	0.5882
New York	62	0.2028	0.2995	0.0026
North Carolina	100	0.1971	0.2184	0.3101
North Dakota	53	0.1562	0.2361	0.0053
Ohio	88	0.1681	0.2241	0.0078
Oklahoma	77	0.2724	0.2180	0.0540
Oregon	36	0.1534	0.2163	0.0458
Pennsylvania	67	0.1692	0.2214	0.0305
Rhode Island	5	0.0830	0.1239	0.4568
South Carolina	46	0.1924	0.2251	0.2962
South Dakota	66	0.2091	0.3476	0.0001
Tennessee	97	0.2136	0.2641	0.0408
Texas	254	0.2744	0.3035	0.0546
Utah	29	0.1732	0.2522	0.0516
Vermont	14	0.0949	0.1934	0.0154
Virginia	84	0.2408	0.3006	0.0490
Washington	39	0.1672	0.2213	0.0880
West Virginia	55	0.2318	0.2436	0.7158
Wisconsin	70	0.1940	0.2177	0.3401
Wyoming	23	0.1623	0.2308	0.0531

NOTES: Per capita income figures are in natural log form. *p*-values are based on a variance ratio test where the null hypothesis is that the value of the ratio of the 1998–1970 standard deviations is unity (against the two-tailed alternative).



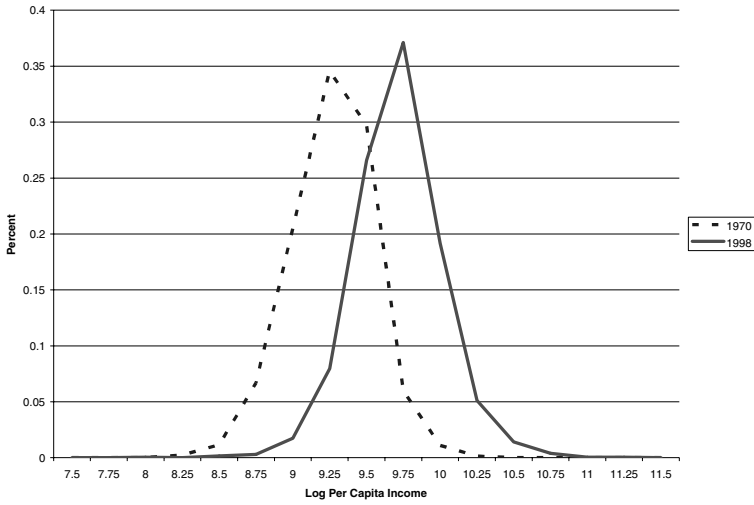


FIG. 2. Distribution of U.S. Counties' Log Per Capita Incomes, 1970 vs. 1998.

TABLE 3

SUMMARY STATISTICS FOR DISTRIBUTION OF U.S. COUNTIES' LOG PER CAPITA INCOMES, 1970 vs. 1998

Statistic	1970 per capita income	1998 per capita income
Standard deviation	0.2728	0.2887
Gini coefficient	0.1666	0.1654
Skewness	-0.2244	1.7240
Kurtosis	3.4334	10.3237

NOTE: Per capita income figures are in natural log form.

To try to understand further the evolution of the U.S. county-level income distribution, Table 3 summarizes two additional statistics computed from the 1970 and 1998 income distributions: skewness and kurtosis. From 1970 to 1998, the skewness of the distribution increased from -0.2244 (to the left) to 1.7240 (to the right). At the same time, kurtosis increased from 3.4334 to 10.3237, implying that the distribution became more peaked. This suggests that these two effects have been offsetting to a great extent.

## 6. CONCLUSION

In this paper, we show that  $\beta$ -convergence is a necessary but *not* sufficient condition for  $\sigma$ -convergence. We discuss evidence of  $\beta$ -convergence in the United States using county-level data for the 1970 to 1998 period. Using the same data, we show that

$\sigma$ -convergence was not present during that time period in the United States or within a large majority of the individual U.S. states considered separately. In many cases, in fact, statistically significant  $\sigma$ -divergence is found.

What are we to make of the presence of  $\beta$ -convergence and evidence of  $\sigma$ -divergence? If the United States was approaching its steady-state income variance from below during the 1970–98 period, then, based on our discussion in Section 2, two interpretations suggest themselves.<sup>13</sup>

First, the initial distribution of income was narrow in 1970 relative to the distribution of balanced growth paths. Second, the 1970 (1998) draw of county-specific shocks had a small (large) sample variance relative to the population variance of shocks.

Going beyond (but still consistent with) the discussion of Section 2, another interpretation is that the variance of the balanced growth paths themselves increased. However, one may consider this second interpretation unlikely considering the relative institutional homogeneity of counties across the United States and especially within individual states where the same  $\beta$ -convergence versus  $\sigma$ -convergence results hold in many cases.

A final—and perhaps least likely—interpretation is that the rich counties tend to have balanced growth *rates* that are higher than those of poor counties. There is little reason to think, however, that the long-run growth rates of technological know-how are different across U.S. counties (and, again, especially within individual states).

In any case, the evolution of skewness and kurtosis suggests that there may be an underlying  $\sigma$ -convergence for a “majority club” of U.S. counties but that there is another “minority club” that is evolving into a long right-hand tail of the distribution, preventing  $\sigma$ -convergence in the aggregate.

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13. A related issue, which we do not address in this paper directly, is whether or not the cross-sectional distribution of log per capita income is ergodic (Evans 1996). That would mean that the cross-sectional variance is stationary around a mean or is converging asymptotically toward a constant mean.

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